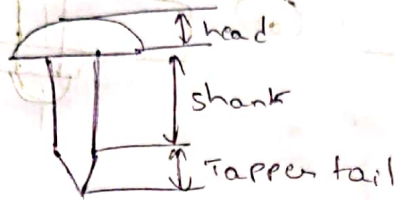


Rivets & welded Joints

Riveted Joint :- A Rivet is a short cylindrical rod having a head & taper tail. The main body of the rivet is called Shank.

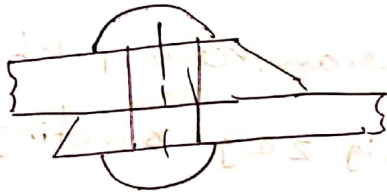


Types of Riveted Joint

1) Lap Joint :-

2) Butt Joint :-

1) Lap joint :- The plates that are to be joined are brought face to face such that an Over lap exist as shown in figure.

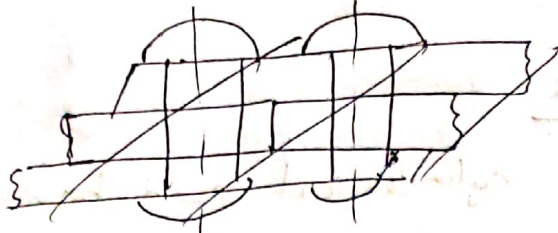


Depending upon the number of row the riveted joints might be classified as, single, double (or) triple riveted lap joint etc.

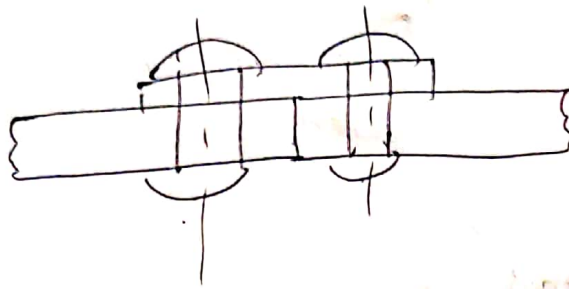
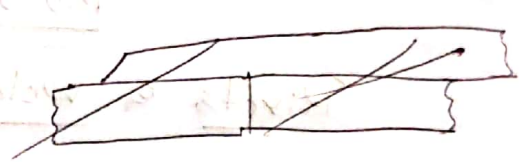
When the multiple joints are used the arrangement of rivets b/w two neighbouring row may be of two kinds. In Chain rivetting the adjacent rows have rivets in the same transverse lines.

In Zig Zag rivetting on the other hand the adjacent row of rivets are staggered.

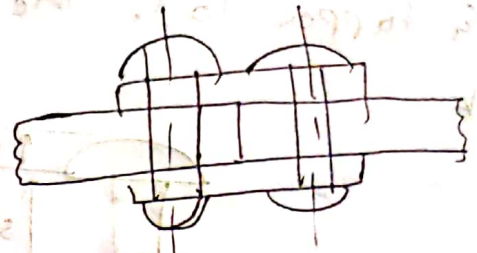
2) Butt Joint :- In this type of joint the plates are brought to ~~each other~~ ^{together} without forming any Over lap. Riveted joints are formed b/w each of plate & one (or) two cover plate.



(a)



(c)



Terminology

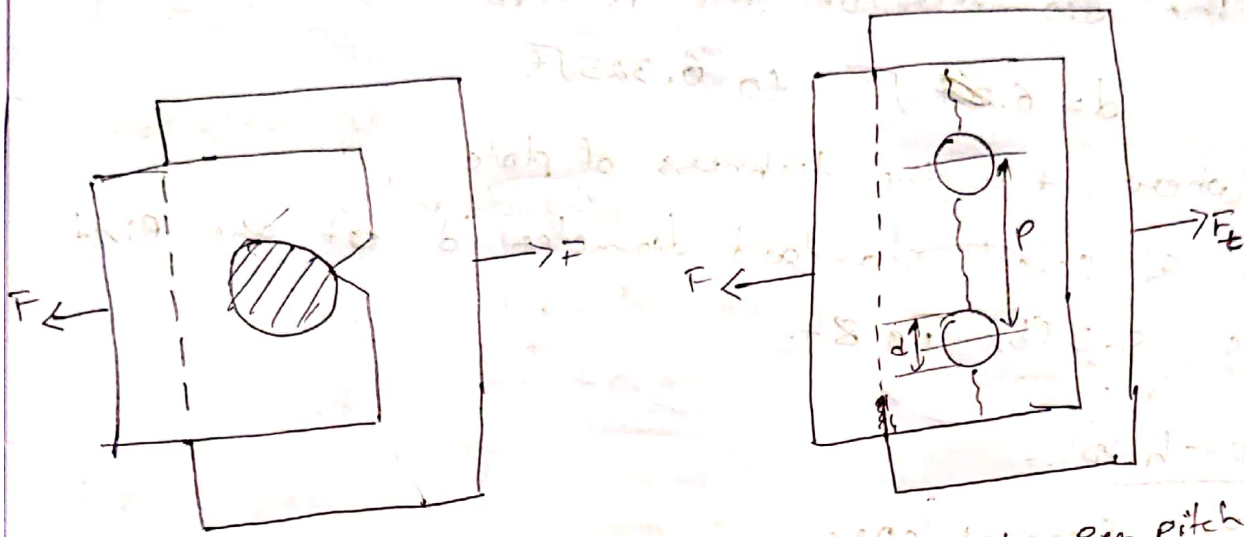
- 1) pitch (P): It is distance b/w the centre of two successive rivets in a row.
- 2) margin (m): It is distance from end of plate to the first row of rivet.
- 3) Transverse pitch (P_t): - The distance b/w two successive row of rivets is called Transverse pitch.
- 4) Diagonal pitch (P_d): - In zig zag riveting the distance b/w centre of adjacent rivets in side by side row is Diagonal pitch.

Modes of failure

Any rivet joint can fail in one (or) more ways as mentioned below.

- 1) Tearing of plate
- 2) Shearing of rivets
- 3) Crushing of rivets

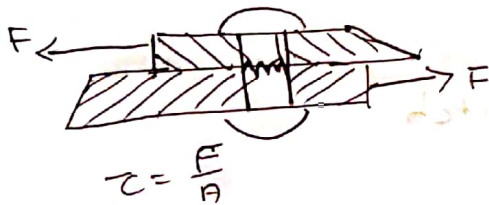
1) Tearing of plate :- The Joint may fail due to tearing of plate at margin (or) Tearing of plate along the line of rivet holes.



Tearing strength per pitch length

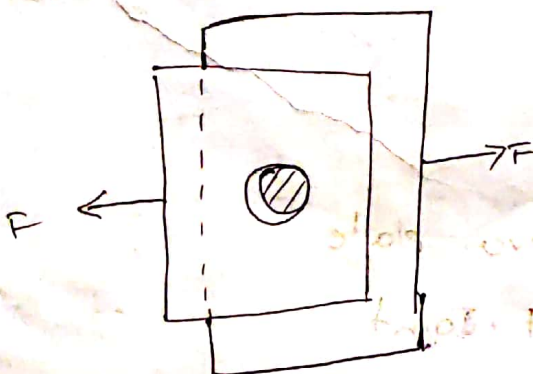
$$F_t = \sigma_t (P - d) t$$

2) shearing of rivets
The Joint may fail due to shearing of rivets as shown in figure.



3) Crushing of rivets :-

When the Joint is loaded compressive stress is induced over a contact area b/w rivets & the plate



Design Procedure: for Rivetted Joint to connect two plates of thickness 't'

Step 1:- The diameter of the Rivet

$$d = 6.0 \sqrt{t} \text{ to } 6.325 \sqrt{t}$$

where, t is the thickness of plate

Find 'd' & select standard diameter 'd' of the Rivet from table 5.3 (b) Pg 84.

Step 2:- Pitch 'P':-

a) In General case

$$P = \frac{(0.1 + 1.875 n_2) \pi d^2 \tau}{4 t \sigma_t} + d \rightarrow 5.12(a) \text{ Pg 81}$$

b) As per IBR (Indian Boiler Regulation) the maximum shorter pitch of the rivet is given by $\therefore P = k_1 t \nless 41 \text{ mm}$

~~$P = k_1 t + 1$~~ where k_1 is constant from table 5.4(a) Pg 85

Take the smaller value of the pitch

Step 3 Transverse pitch ' P_t ':-

$$P_t = 2.5 d \quad [\text{range } 2d - 2.5d]$$

Step 4

$$\text{margin (m)} = 1.5 d$$

Step 5

Thickness of cover plate

a) For lap Joint no cover plate

b) For single cover butt Joint

$$\therefore t_1 = 1.125 t \rightarrow 5.4(a) \text{ Pg 79}$$

c) For double cover plates with equal cover

$$t_i = 0.625t \rightarrow 5.4(c) \text{ Pg } 80$$

d) For double cover plates with unequal cover

✓ Thickness of narrow plate

$$t_o = 0.625t \rightarrow 5.4(c) \text{ Pg } 80$$

✓ Thickness of wider plate

$$t_i = 0.75t \rightarrow 5.4(c) \text{ Pg } 80$$

Step 4 Efficiency of Joint

i) efficiency of plate

$$\eta_p = \frac{P-d}{P} \rightarrow 5.9(E) \text{ Pg } 81$$

ii) efficiency of rivet in shear

$$\eta_s = \frac{\pi/4 \cdot d^2 (n_1 + 1.875 n_2) \tau}{P t \sigma_t} \rightarrow 5.9(f) \text{ Pg } 81$$

iii) efficiency of rivet in crushing

$$\eta_c = \frac{(n_1 t_i/t + n_2) \sigma_c}{(n_1 t_i/t + n_2) \sigma_c + \sigma_t} \rightarrow 5.7 \text{ Pg } (80)$$

To find efficiency of lap joint

$$\text{Put } t_i/t = 1 \text{ \& } n_2 = 0$$

The efficiency of Rivetted Joint is the least of above three value the joint fails where every efficiency is minimum.

Problem

i) Design a double rivetted lap joint to connect two plates each 80mm thick. The allowable stress for rivet & plate are 90MPa in tension & 60MPa in shear & 150MPa in crushing.

Soln:- Double rivetted lap joint

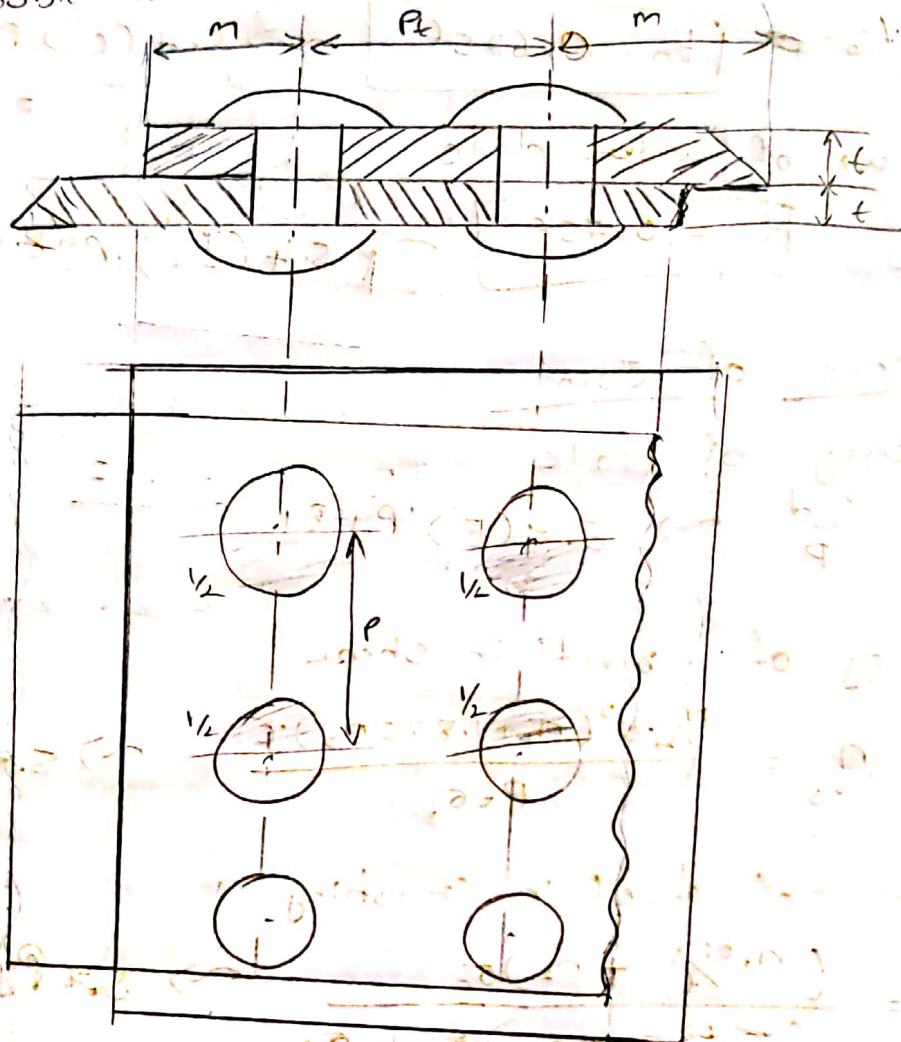


Figure shows double lap joint since the type of Rivetting is not mentioned. A Chain type of Rivet is assumed.

consider one Pitch length mark as P & theoretically no. of rivets per Pitch length

✓ In line 1 $\frac{1}{2} + \frac{1}{2} = 1$ (Rivet in single shear)

✓ In line 2 $\frac{1}{2} + \frac{1}{2} = 1$ (Rivet in single shear)

Total no. of Rivets per pitch length in single shear

$$n_1 = 1 + 1 = 2$$

Double shear $n_s = 0$

$$t = 20 \text{ mm}$$

$$\sigma_t = 90 \text{ MPa}, \quad \tau = 60 \text{ MPa}$$

$$\sigma_c = 150 \text{ MPa}$$

$$i) d = 6 \sqrt{t} \text{ to } 6.325 \sqrt{t}$$

$$d = 6 \sqrt{20} \text{ to } 6.325 \sqrt{20}$$

$$\therefore d = \underline{26.8328 \text{ mm}} \text{ to } \underline{28.2862 \text{ mm}}$$

From Table S.3(b) Pg 84 standard diameter of rivet

$$d = 27 \text{ mm}$$

$$ii) q/p = \frac{(n_1 + 1.875 n_2) \pi d^2 \tau}{4 t \sigma_t} + d$$

$$P = \frac{(2 + 0) \pi (27)^2 \times 60}{4 \times 20 \times 90} + 27$$

$$P = \underline{65.1703 \text{ mm}} \approx \underline{66 \text{ mm}}$$

$$b) P = k_1 t + 41 \text{ mm}$$

From table S.4 (a) Pg 85

For no. of rivets

$$k_1 = 2.62$$

$$P = 2.62 \times 20 + 41 \text{ mm}$$

$$P = \underline{93.4 \text{ mm}}$$

The smaller value of the pitch = 66 mm (choose shorter value)

$$iii) P_t = 2.25 d = 2.25 \times 27$$

$$P_t = 60.75 \text{ mm} \approx \underline{61 \text{ mm}}$$

iv) a) efficiency of plate

$$\eta_p = \frac{P - d}{P} = \frac{66 - 27}{66} = \underline{59.09\%}$$

b) efficiency of rivet in shear

$$\eta_s = \frac{\pi d^2/4 (n_1 + 1.875 n_2) \tau}{P + \sigma_t}$$

$$= \frac{11 \times 27^2/4 (2 + 0) 90}{66 \times 20 \times 90}$$

$$\eta_s = 0.5183$$

$$\boxed{\eta_s = 51.83\%}$$

c) efficiency of rivet in crushing

$$\eta_c = \frac{(n_1 t_1 + n_2 t_2) \sigma_c}{(n_1 t_1 + n_2 t_2) \sigma_c + \sigma_t}$$

For lap joint $t_1/t_2 = 1$

$$\eta_c = \frac{(2 + 0) 150}{(2 + 0) 150 + 90}$$

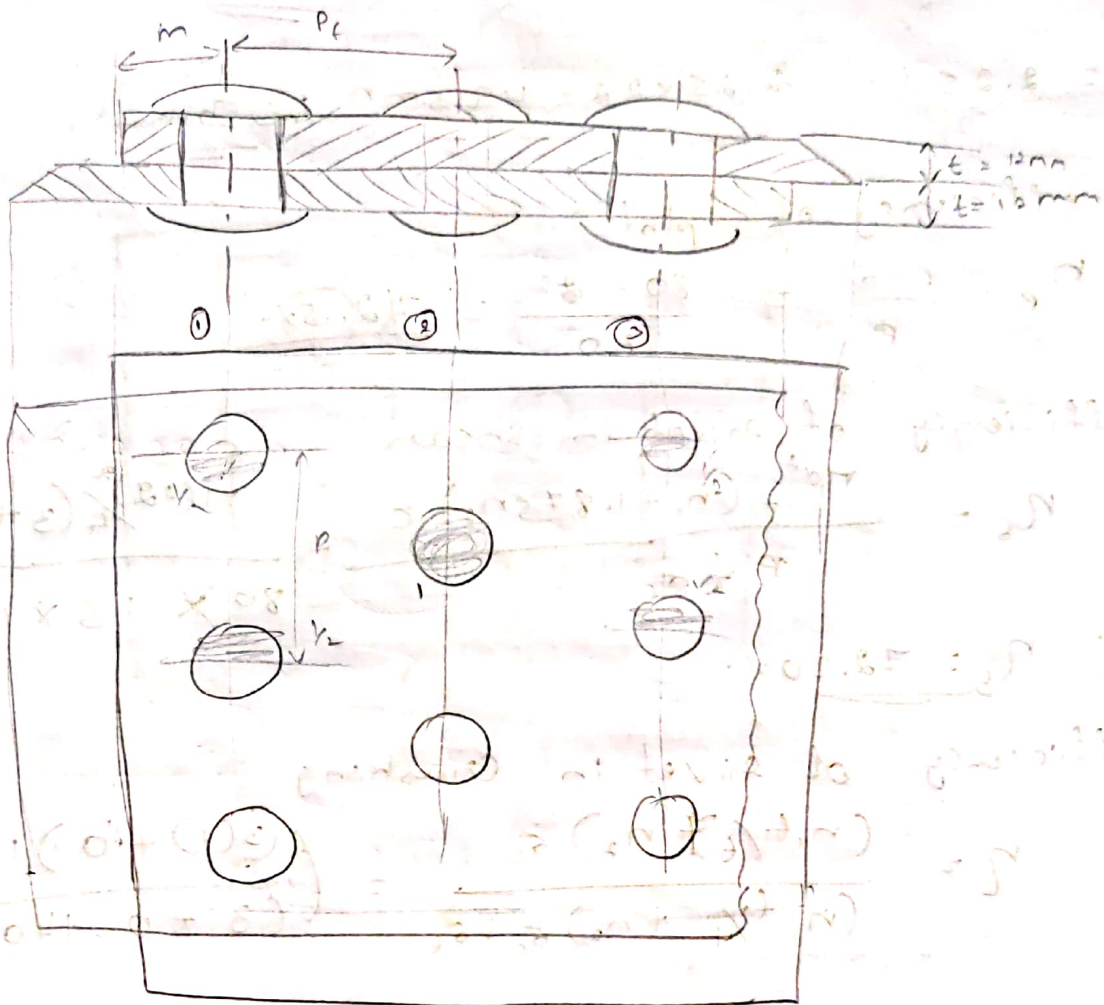
$$\eta_c = 0.7692$$

$$\boxed{\eta_c = 76.92\%}$$

(Suggest small efficiency value)

Efficiency of the lap joint = 51.83%

Q) Design a triple rivetted zig zag lap joint to connect two plates each 12mm thick. Draw a neat sketch of the joint. Take $\sigma_t = 115 \text{ MPa}$, $\tau = 70 \text{ MPa}$, & $\sigma_c = 140 \text{ MPa}$.



Total no of Rivets per pitch length in sing shear

$$n_1 = 1 + 1 + 1 = \underline{\underline{3}}$$

Double shear $n_2 = 0$

$$t = 12 \text{ mm}$$

$$\sigma_t = 115 \text{ MPa}$$

$$\tau = 70 \text{ MPa}$$

$$\sigma_c = 140 \text{ MPa}$$

$$\therefore d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$= 6 \times \sqrt{12} \text{ to } 6.325\sqrt{12}$$

$$d = 20.784 \text{ mm to } 21.91 \text{ mm}$$

From Table S.3(b) pg 84

standard diameter of rivet

$$\underline{\underline{d = 22 \text{ mm}}}$$

$$\text{ii) a) } p = \frac{(n_1 + 1.87n_2)\pi d^2 \tau + d^2 \sigma_c}{4t\sigma_t}$$

$$p = \frac{(3 + 1.87(0))\pi(22)^2 \times 70 + 22^2 \times 140}{4 \times 12 \times 115}$$

$$p = \underline{\underline{79.84628 \text{ mm}}}$$

$$\text{b) } p = k_t t + 41 \text{ mm}$$

From table S.4(a) pg 85

For no of rivets

$$k_t = 3.47$$

$$p = 3.47 \times 12 + 41$$

$$\therefore p = \underline{\underline{82.64 \text{ mm}}}$$

The smallest value of pitch = $p = 19.8462 \text{ mm} \approx \underline{80 \text{ mm}}$

iii) $P_t = 2.25d = 2.25 \times 22 = \underline{49.5 \text{ mm}} \approx \underline{50 \text{ mm}}$

iv) a) efficiency of plate

$$\eta_p = \frac{p-d}{p} = \frac{80-22}{80} = \underline{72.5\%}$$

b) efficiency of rivet in shear

$$\eta_b = \frac{n d^2 / 4 (n_1 + 1.875 n_2) \tau}{p \times \sigma_t} = \frac{7(22)^2 / 4 (3 + 1.875(0)) \tau}{80 \times 115 \times 12}$$

$$\therefore \eta_b = \underline{72.30\%}$$

c) efficiency of rivet in crushing

$$\eta_c = \frac{(n_1 t_1 / e + n_2) \sigma_c}{(n_1 t_1 / e + n_2) \sigma_c + \sigma_t} = \left(\frac{(3(1) + 0) 140}{(3 + 0) 140 + 115} \right)$$

$$\therefore \eta_c = \underline{78.50\%}$$

(suggest the smallest efficiency value)

Efficiency of the lap joint = 42.3%

3) Design single rivetted single cover butt joint to connect two plates 30mm thick. The yield stress for plate & rivet material is 324MPa use FOS of 2.5 for tension, 4 for shear & 2 for crushing.

Solⁿ :- $t = 30 \text{ mm}$

$$\sigma_y = 324 \text{ MPa}$$

$$\eta_t = 2.5$$

$$\eta_c = 2$$

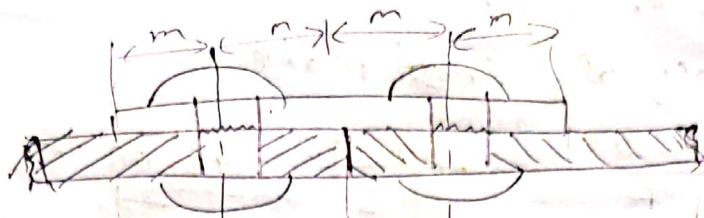
$$\eta_s = 4$$

$$\sigma_t = \frac{\sigma_y}{\eta_t} = \frac{324}{2.5}$$

$$\boxed{\sigma_t = 129.6 \text{ MPa}}$$

$$\tau_s = \frac{\sigma_y}{\eta_s} = \frac{324}{4}$$

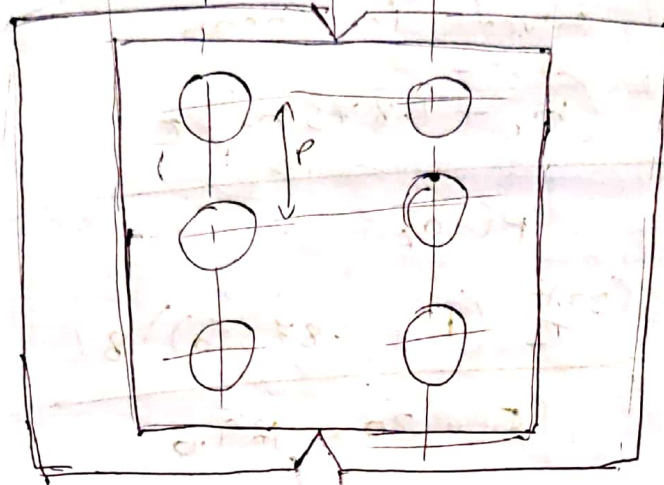
$$\boxed{\tau_s = 81 \text{ MPa}}$$



$$\sigma_c = \frac{\sigma_y}{2} = \frac{324}{2}$$

$$\sigma_c = 162 \text{ MPa}$$

$$t = 30 \text{ mm}$$



$$n_1 = 1$$

$$n_2 = 0$$

$$i) \text{ diameter} = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 6\sqrt{30} \text{ to } 6.325\sqrt{30}$$

$$d = 32.8633 \text{ to } 34.643 \text{ mm}$$

$$\therefore d = 33 \text{ mm} \quad \text{From table 5.3(b) Pg 84}$$

$$ii) a) p = \frac{(n_1 + 1.875n_2) \pi d^2 \tau}{4t\sigma_c} + d$$

$$= \frac{(1 + 1.875(0)) \pi (33^2) 81}{4 \times 30 \times 129.6} + 33$$

$$\therefore p = 50.81872 \text{ mm}$$

$$b) p = k_1 t + 44 \text{ mm}$$

$$k_1 = 1.53 \quad \text{Table 5.4 Pg 85}$$

$$p = 1.53 \times 30 + 44 \text{ mm}$$

$$p = 89.9 \text{ mm}$$

$$\text{the smaller value of pitch } p = 50.8187 \text{ mm} \approx 51 \text{ mm}$$

$$iii) \text{ margin } (m) = 1.5d = 1.5 \times 33 = 49.5 \text{ mm} \approx 50 \text{ mm}$$

$$iv) t_i = 1.125t = 1.125 \times 30$$

$$t_i = 33.75 \text{ mm} = 34 \text{ mm}$$

efficiency of joint
 W) efficiency of ~~cover~~ plate

$$\eta_r = \frac{p-d}{p} = \frac{51-33}{51} = \underline{35.29\%}$$

b) efficiency of rivet in shear

$$\eta_b = \frac{\frac{\pi d^2}{4} (n_1 + 1.875 n_2) \tau}{p t \sigma_t}$$

$$= \frac{\pi \frac{(33)^2}{4} (1 + 1.875(0)) 81}{51 \times 30 \times 129.6}$$

$$\eta_b = 0.3493 = \underline{34.93\%}$$

c) efficiency of rivet in crushing

$$\eta_c = \frac{(n_1 (t/t) + n_2) \sigma_c}{(n_1 t/t + n_2) \sigma_c + \sigma_c}$$

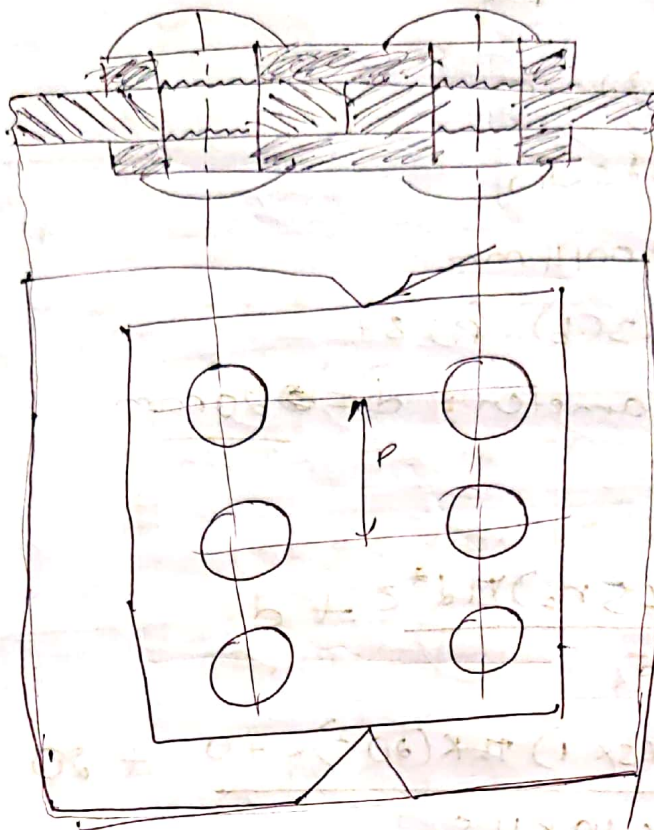
$$\eta_c = \frac{(1 (34/30) + 0) 162}{(1 (34/30) + 0) 162 + 129.6}$$

$$\eta_c = 0.586207$$

$$\boxed{\eta = 58.62\%}$$

efficiency of Joint $\eta = 34.93\%$

4) single riveted Butt Joint with double cover Plate.



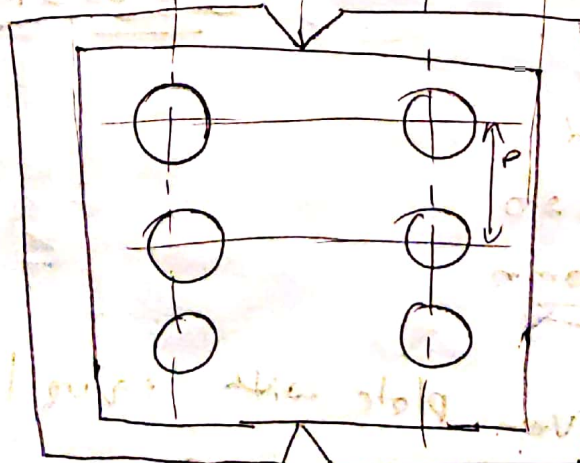
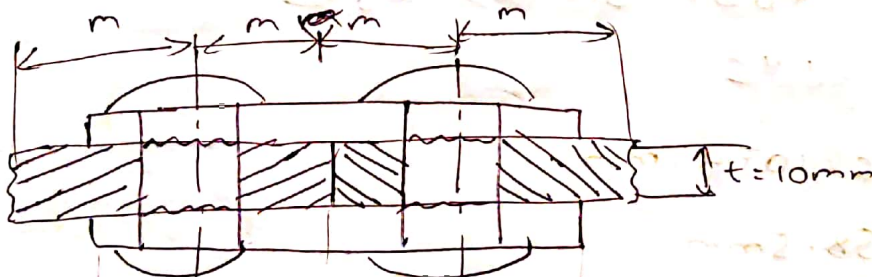
Double shear so

$$n_1 = 0$$

For Double shear

$$n_2 = 1$$

5) Design a single rivetted double cover butt joint to connect two plates 10mm thick. Take allowable tensile stress 115 MPa & $\tau_{all} = 40 \text{ MPa}$ & allowable crushing stress 140 MPa



For Double shear

$$n_1 = 0$$

$$n_2 = 1$$

$$\sigma_{tall} = 115 \text{ MPa}$$

$$\tau_{all} = 40 \text{ MPa}$$

$$\sigma_c = 140 \text{ MPa}$$

✓ The diameter of the rivet

$$d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 6\sqrt{10} \text{ to } 6.325\sqrt{10}$$

$$d = 18.973 \text{ to } 20.0014 \text{ mm}$$

From the table 5.3(b) pg 84

the standard diameter = $d = 20 \text{ mm}$

Pitch

$$a) P = \frac{(n_1 + 1.875n_2)\pi d^2 \times 70}{4t\sigma_t} + d$$

$$P = \frac{(0 + 1.875 \times 1)\pi \times (20)^2 \times 70}{4 \times 10 \times 115} + 20$$

$$P = 55.855 \text{ mm}$$

$$b) P = k_1 t + 41 \text{ mm}$$

From table 5.4(a) pg 85

$$k_1 = 1.75$$

$$P = 1.75 \times 10 + 41 \text{ mm}$$

$$P = 58.5 \text{ mm}$$

the smallest pitch value $P = 55.855 \text{ mm}$

$$\text{margin (m)} = 1.5 \times d$$

$$= 1.5 \times 20$$
$$= 30 \text{ mm}$$

c) For double cover plate with eq. 1

$$f_1 = 0.625f = 0.625 \times 10$$

$$f_1 = 6.25 \text{ mm}$$

✓ Efficiency of riveted joint

$$\eta_p = \frac{P - d}{P} = \frac{55.855 - 20}{55.855}$$

$$\boxed{\eta_p = 64.19\%}$$

$$ii) \eta_s = \frac{\pi/4 d^2 (n_1 + 1.875 n_2) \tau}{P \sigma_t}$$

$$= \frac{\frac{\pi}{4} \times (20)^2 (0 + 1.875 \times 1) \tau}{55.855 \times 10 \times 115}$$

$$\boxed{\eta_s = 64.19\%}$$

$$iii) \eta = \frac{(n_1 t_1/t + n_2) \sigma_c}{(n_1 t_1/t + n_2) \sigma_t + \sigma_c}$$

$$\eta = \frac{(0 + 1) 140}{(0 + 1) 140 + 115}$$

$$\boxed{\eta = 54.90\%}$$

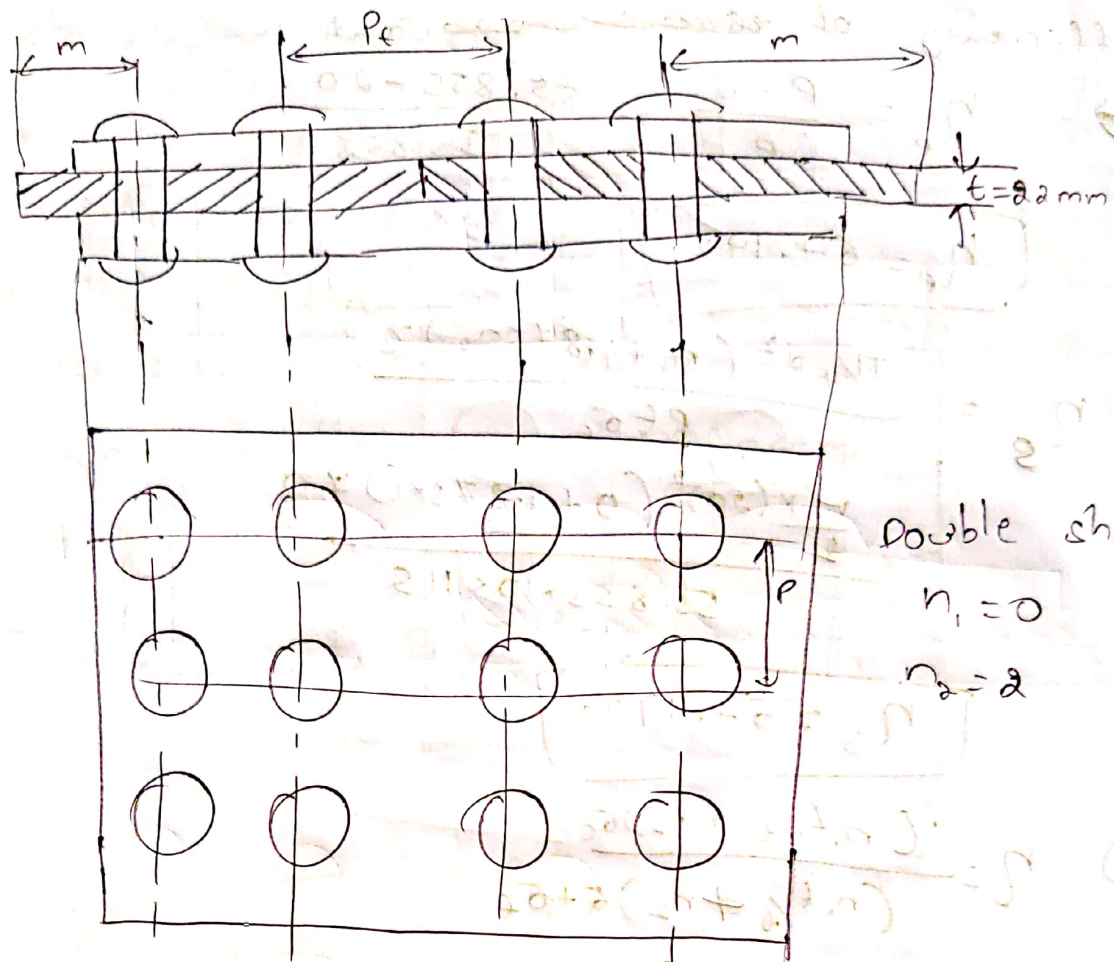
efficiency of the butt joint = 54.90%

6) Double riveted Butt joint with double cover plates equal plate thick 22mm,

$$\sigma_t = 90 \text{ MPa}$$

$$\tau = 60 \text{ MPa}$$

$$\sigma_c = 150 \text{ MPa}$$



Double shear

$$n_1 = 0$$

$$n_2 = 2$$

$$\checkmark d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 6\sqrt{8.2} \text{ to } 6.325\sqrt{8.2}$$

$$d = 28.14 \text{ to } 29.66 \text{ mm}$$

From table 5.3(b) Pg 84

The standard diameter $d = \underline{30 \text{ mm}}$

- Pitch

$$a) p = \frac{(n_1 + 1.875n_2) \pi d^2}{4t + 5t} + d = \frac{(0 + 1.875 \times 2) \pi (30^2) \times 60}{4 \times 8.2 + 5 \times 90}$$

$$p = \underline{110.3248 \text{ mm}}$$

$$b) p = k_1 t + 44 \text{ mm}$$

From table 5.12(b) Pg 85

$$k_1 = 3.5$$

$$p = 3.5 \times 8.2 + 44$$

$$p = \underline{121 \text{ mm}}$$

one smallest pitch value $P = 110.3248 \approx \underline{111 \text{ mm}}$

$$\checkmark P_t = 2.25d = 2.25 \times 30 = \underline{67.5 \text{ mm}}$$

$$\checkmark \text{margin, } m = 1.5 \times 30 = \underline{45 \text{ mm}}$$

~~also~~ For double cover plate with equal

$$t_i = 0.625t = 0.625 \times 22$$

$$t_i = \underline{13.75 \text{ mm}}$$

$$\checkmark \text{ i) } \eta_p = \frac{P-d}{P} = \frac{111 - 30}{111} = \underline{72.97\%}$$

$$\text{or ii) } \eta_s = \frac{\frac{\pi d^2}{4} (n_1 + 1.875 n_2) \tau}{P t \sigma_t} = \frac{\frac{\pi \times (30)^2}{4} (0 + 1.875 \times 2) 60}{111 \times 22 \times 90}$$

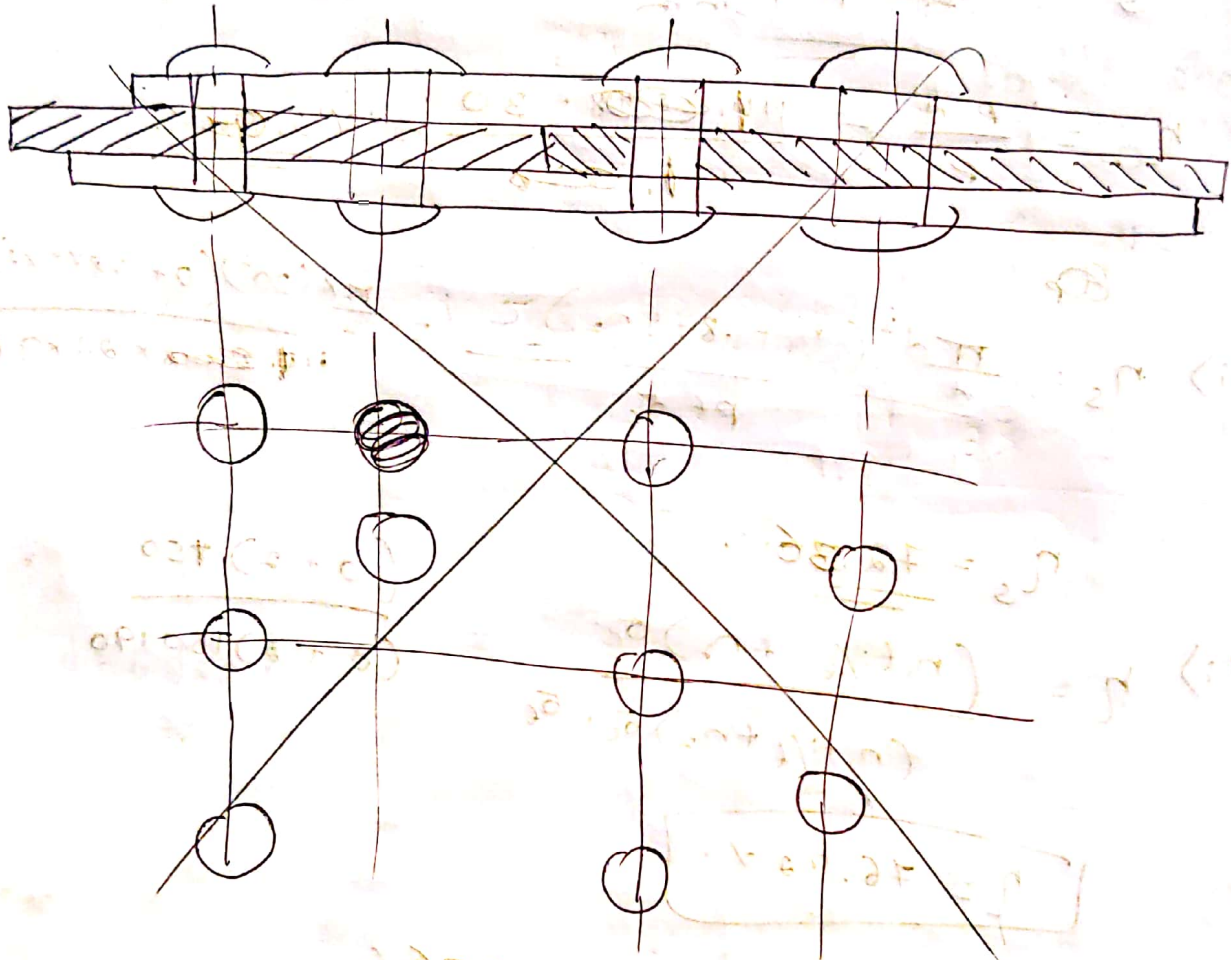
$$\eta_s = \underline{72.36\%}$$

$$\text{iii) } \eta = \frac{(n_1 t_i/t + n_2) \sigma_c}{(n_1 t_i/t + n_2) \sigma_c + \sigma_t} = \frac{(0 + 2) 150}{(0 + 2) 150 + 90}$$

$$\boxed{\eta = 76.92\%}$$

Efficiency of Bolt Joint = 72.36%

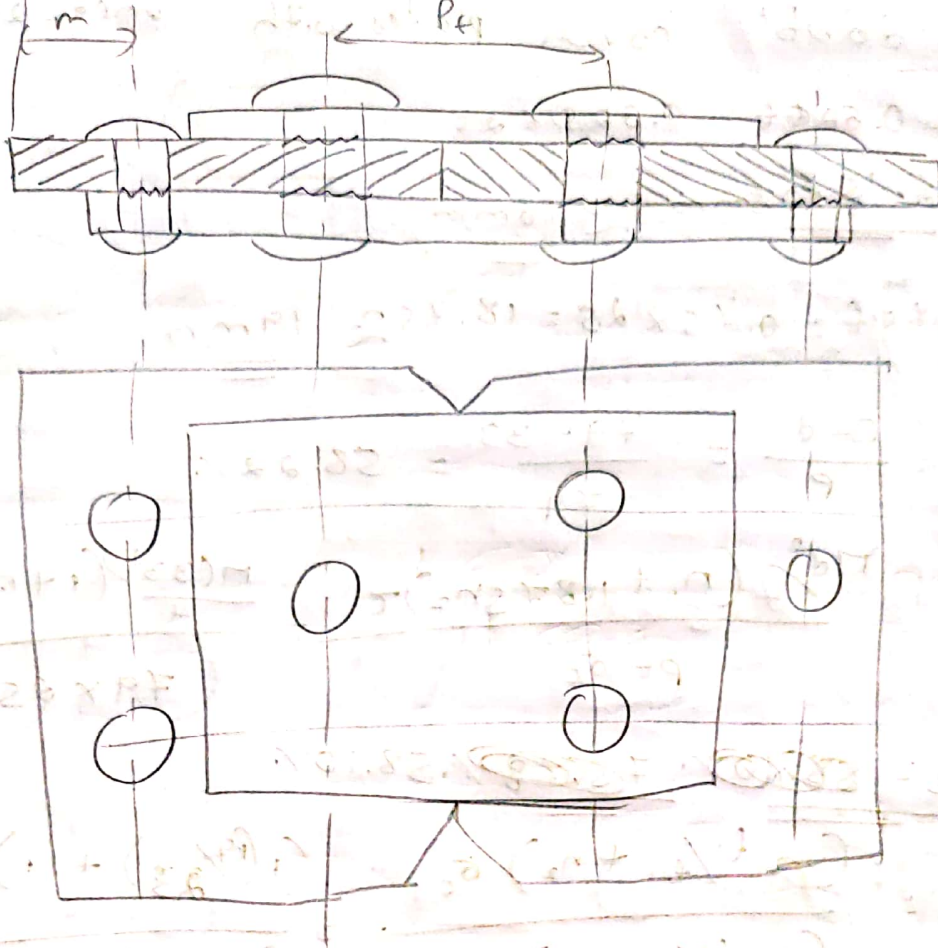
~~Double Rivetted Bolt Joint, Double cover plate with unequal lengths zig zag arrangement~~



7) Design a double riveted double cover Butt joint with unequal cover & zig zag riveting to connect two plates of 25mm thick assume $\sigma_t = 150 \text{ MPa}$

$$\tau = 70 \text{ MPa}$$

$$\sigma_c = 140 \text{ MPa}$$



$$n_1 = 1$$

$$n_2 = 1$$

$$d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 6\sqrt{25} \text{ to } 6.325\sqrt{25}$$

$$d = 30 \text{ to } 31.625 \text{ mm}$$

From Table 5.3(b) pg 84

the standard diameter, $d = 33 \text{ mm}$

✓ pitch

$$a) P = \frac{(n_1 + 1.875n_2)\pi d^2 \tau}{4 + \sigma_c} + d = \frac{(1 + 1.875 \times 1)\pi (33^2) \times 70}{4 \times 25 \times 150} + 33$$

$$P = \underline{\underline{78.9010 \text{ mm}}}$$

$$P = k_1 t + 44 \text{ mm}$$

From the table 5.4(a) pg 85

$$k_1 = 3.5$$

$$P = 3.5 \times 25 + 44 \text{ mm} = 131.5 \text{ mm}$$

the smallest pitch value = $78.9010 \text{ mm} \approx \underline{\underline{79 \text{ mm}}}$

$$✓ P_b = 2.25d = 2.25 \times 33 = \underline{\underline{74.25 \text{ mm}}} \approx \underline{\underline{75 \text{ mm}}}$$

$$✓ m = 1.5d = 1.5 \times 33 = \underline{\underline{49.5 \text{ mm}}} \approx \underline{\underline{50 \text{ mm}}}$$

✓ For double cover plates with unequal cover

$$t_0 = 0.625t = 0.625 \times 25$$

$$t_0 = 15.625 \text{ mm} \approx 16 \text{ mm}$$

$$t_1 = 0.75t = 0.75 \times 25 = 18.75 \approx 19 \text{ mm}$$

$$i) \eta_p = \frac{P-d}{P} = \frac{79-33}{79} = 58.22\%$$

$$ii) \eta_s = \frac{\pi d^2}{4} (n_1 + 1.875 n_2) \tau = \frac{\pi (33^2)}{4} (1 + 1.875 \times 1) \tau$$

$$79 \times 25 \times 140$$

$$\eta_s = 58.10\%$$

$$iii) \eta = \frac{(n_1 t_1/t + n_2) \sigma_c}{(n_1 t_1/t + n_2) \sigma_c + \sigma_t} = \frac{(1(19/25) + 1) 140}{(1(19/25) + 1) 140 + 150}$$

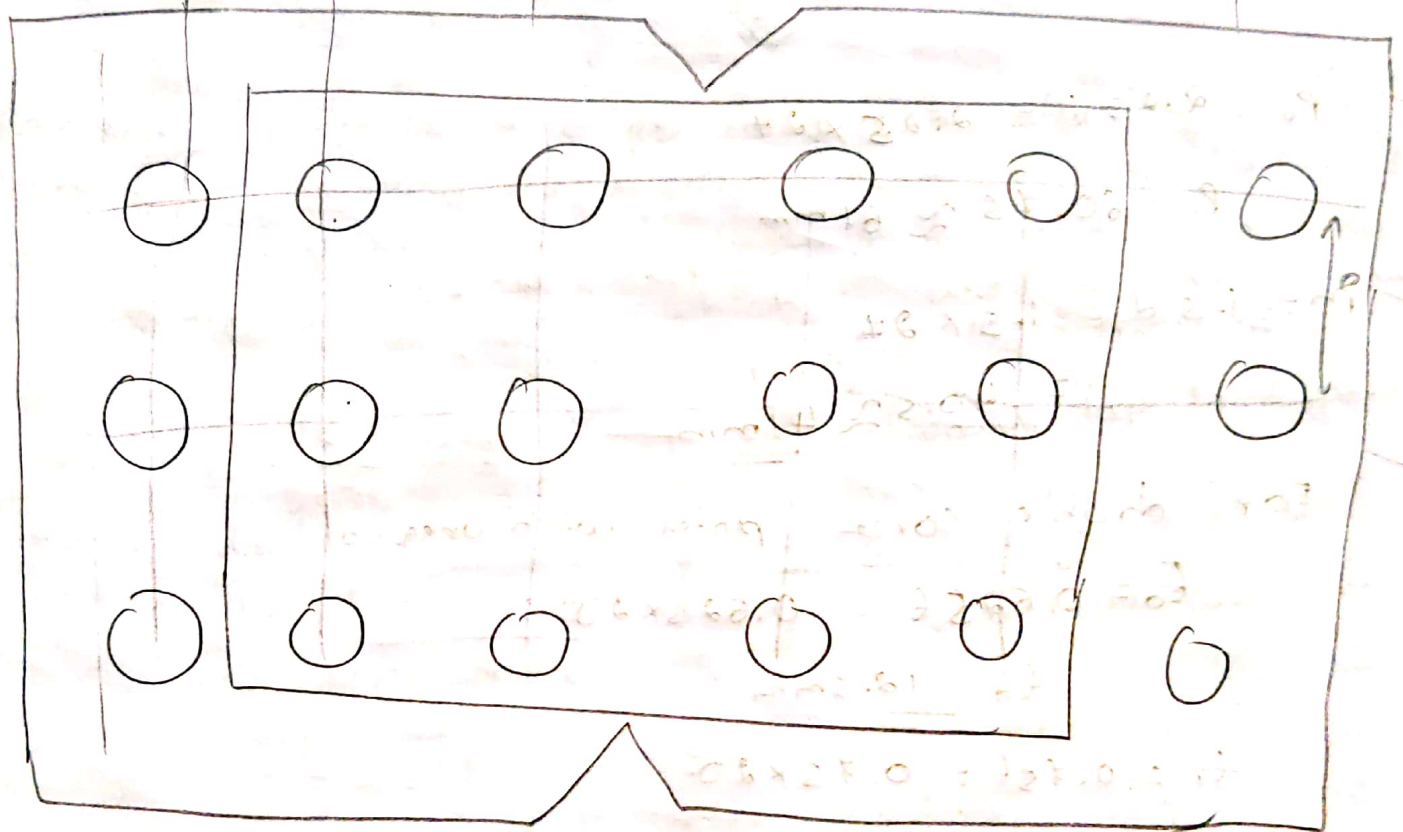
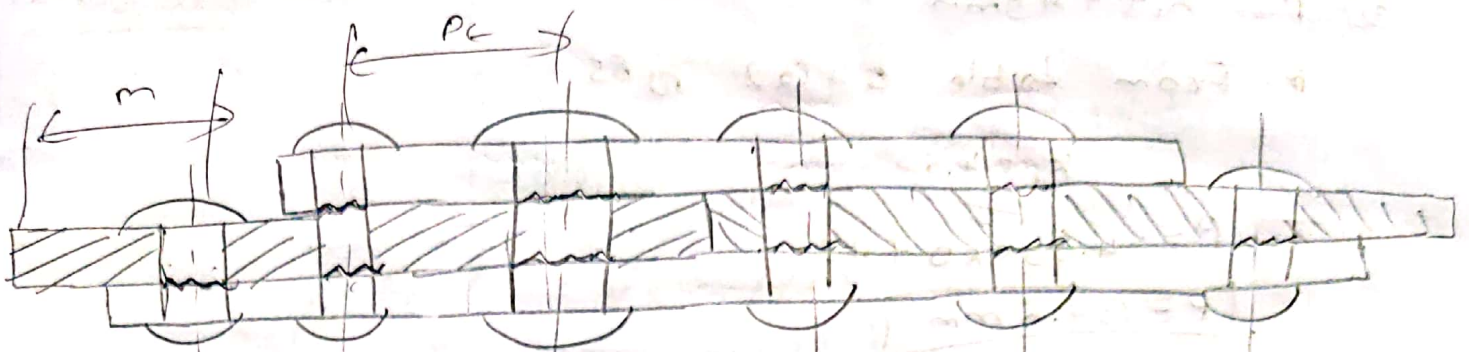
$$\eta = 68.17\%$$

$$\eta = 58.22\%$$

8) Design a Triple rivetted Butt Joint unequal cover plate with unequal cover plate to connect two plates of 20 mm thickness, $\sigma_t = 90 \text{ MPa}$

$$\tau = 60 \text{ MPa}$$

$$\sigma_c = 150 \text{ MPa}$$



$$\left. \begin{matrix} n_1 = 1 \\ n_2 = 2 \end{matrix} \right\} \begin{matrix} n_1 = 1 \\ n_2 = 2 \end{matrix}$$

$$d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 6\sqrt{20} \text{ to } 6.325\sqrt{20}$$

$$d = 26.83 \text{ to } 28.288 \text{ mm}$$

From Table 5.3 (b) pg 84

the standard diameter is 24 mm

pitch

$$a) \quad p = \frac{(n_1 + 1.875n_2) \pi d^2}{4t\sigma_t} + d = \frac{(1 + 1.875 \times 2) \pi \times 24^2 \times 60}{4 \times 20 \times 90} + 24$$

$$p = 117.65 \approx 118 \text{ mm}$$

$$b) P = k_1 t + 45 \text{ mm}$$

From table 9.4 (a) pg 85

$$k_1 = 4.63$$

$$P = 4.63 \times 20 + 45$$

$$P = 137.6 \text{ mm}$$

The smallest pitch value $P = 118 \text{ mm}$.

$$\checkmark P_e = 2.25 d = 2.25 \times 24$$

$$P_e = 60.75 \approx 61 \text{ mm}$$

$$\checkmark m = 1.5 d = 1.5 \times 24$$

$$= 40.5 \approx 41 \text{ mm}$$

For double cover plates with unequal

$$t_o = 0.625 t = 0.625 \times 20$$

$$t_o = 12.5 \text{ mm}$$

$$t_i = 0.75 t = 0.75 \times 20$$

$$t_i = 15 \text{ mm}$$

$$\checkmark i) \eta_p = \frac{P - d}{P} = \frac{118 - 24}{118}$$

$$\eta_p = 79.11 \%$$

$$ii) \eta_s = \frac{\pi d^2 / 4 (n_1 + 1.875 n_2) \sigma_c}{P t \sigma_c}$$

$$\eta_s = \frac{11 \times 24^2 / 4 (1 + 1.875 \times 2) 60}{118 \times 20 \times 90}$$

$$iii) \eta = \frac{(n_1 t_i / t + n_2) \sigma_c}{(n_1 t_i / t + n_2) \sigma_c + \sigma_c}$$

$$\eta_s = 76.82 \%$$

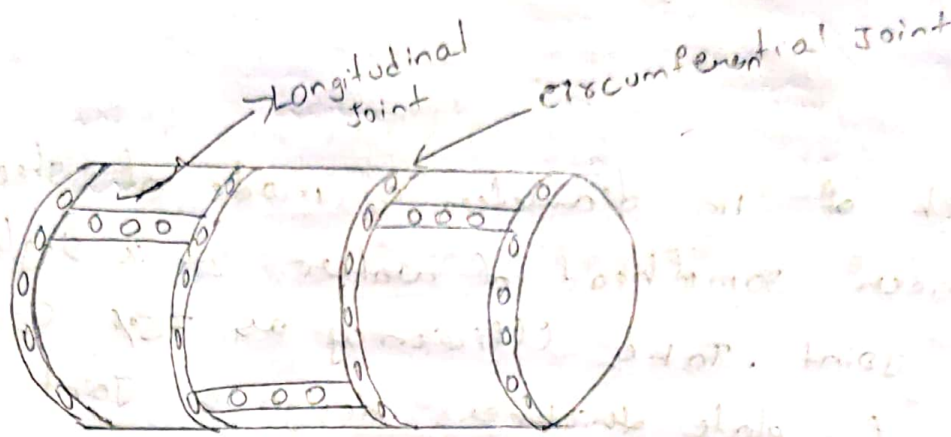
$$\eta = \frac{1(15/20) + 2(150)}{(1(15/20) + 2(150) + 90}$$

$$\eta = 82.08 \%$$

the efficiency of bolt joint

$$\eta = 76.82 \%$$

Pressure vessels :-



Pressure vessels are generally fabricated by joining several plates using the rivetted joint. The rivetted joint which is used to form a cylinder is known as longitudinal joint. The rivetted joint which is used to connect two cylinders are known as circumferential joint.

one circumferential joint is always lap joint (preferable double rivetted).
one longitudinal joint is always butt joint (preferable triple rivetted with unequal cover plate).

Design procedure for Boiler joint :-

1) Longitudinal joint :-

a) Thickness of plate, $t = \frac{P \cdot D}{2 \sigma \eta} + C \rightarrow [eq. 1 pg 79]$

where P is pressure acting inside the cylinder (or) boiler

D Internal diameter of pressure vessels.

η Efficiency of longitudinal joint.

C Corrosion allowance range 1 to 3 mm

b) Diameter of the rivet

$$d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

select standard diameter using table on DHB

e) pitch

same as designing in rivet.

problem

A penstock of 1m diameter & made of steel plates is operated under 30m of head of water. It is single Rivetted longitudinal joint. Take efficiency as 75% & 2mm corrosion allowance for plate thickness design a joint. The following allowable stresses may be use. $\sigma_t = 120 \text{ MPa}$, $\tau = 96 \text{ MPa}$, $\sigma_c = 162 \text{ MPa}$.

Sol:-

$$D = 10 \text{ m} = 1000 \text{ mm}$$

$$\text{head of water} = 30 \text{ m} = 3 \text{ bar} = 0.3 \text{ MPa}$$

longitudinal joint & single rivetted

$$\eta = 0.75$$

$$C = 2 \text{ mm}$$

$$\sigma_t = 120 \text{ MPa}$$

$$\tau = 96 \text{ MPa}$$

$$\sigma_c = 162 \text{ MPa}$$

[10m of head of water = 1 bar = 0.1 MPa]

$$\tau = 96 \text{ MPa}$$

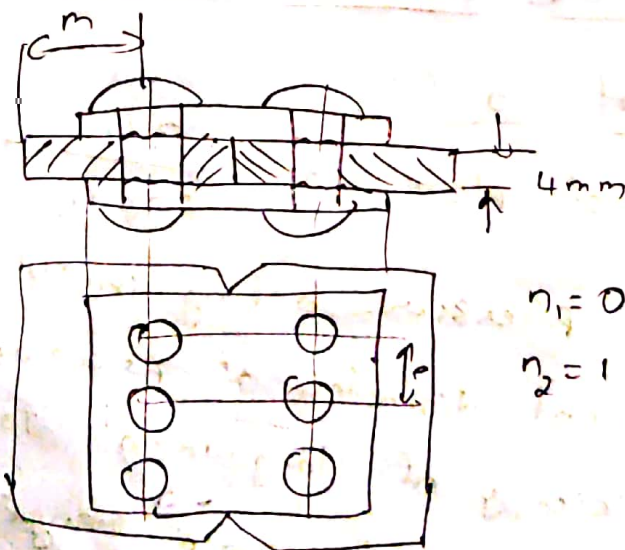
$$\sigma_c = 162 \text{ MPa}$$

$$t = ?$$

$$t = \frac{P \cdot D}{2 \sigma_t \eta} + C$$

$$t = \frac{0.3 \times 1000}{2 \times 120 \times 0.75} + 2$$

$$\therefore t = 3.667 \text{ mm} \approx 4 \text{ mm}$$



$$\eta_1 = 0$$

$$\eta_2 = 1$$

✓ Diameter

$$d = 0.075 \sqrt{t} \text{ to } 6.325 \sqrt{t}$$

$$d = 6 \sqrt{t} \text{ to } 6.325 \sqrt{t}$$

$$d = 12.60 \text{ to } 12.65 \text{ mm}$$

From the table S.3(b) pg 84

The standard diameter $d = 12 \text{ mm}$

✓ pitch 'p'

$$Q) P = \frac{(n_1 + 1.875n_2) \pi d^2 \sigma_c}{4t \sigma_c} + d$$

$$P = \frac{(0 + 1.875 \times 1) \pi \times (12)^2 \times 96}{4 \times 4 \times 120} + 12$$

$$P = \underline{54.4115 \text{ mm}}$$

$$b) P = k_1 t + 41 \text{ mm}$$

From table S.4 (a) pg 85

$$k_1 = 1.53$$

$$P = 1.53 \times 4 + 41 \text{ mm}$$

$$P = \underline{47.12 \text{ mm}} \approx \underline{48 \text{ mm}}$$

The smallest pitch value $P = \underline{48 \text{ mm}}$

$$✓ \text{ margin } m = 1.5d = 1.5 \times 12 = 18 \text{ mm}$$

✓ For double cover plates with equal

$$t_i = 0.625t = 0.625 \times 4 = \underline{2.5 \text{ mm}}$$

$$✓ i) \eta_p = \frac{P-d}{P} = \frac{48-12}{48} = 75\%$$

$$ii) \eta_s = \frac{\pi d^2/4 (n_1 + 1.875n_2) \tau}{P t \sigma_s} = \frac{\pi \times 12^2/4 (0 + 1.875 \times 1) 96}{48 \times 4 \times 120}$$

$$\eta_s = 88.35\%$$

$$iii) \eta = \frac{(n_1 t_i/t + n_2) \sigma_c}{(n_1 t_i/t + n_2) \sigma_c + \sigma_s} = \frac{(0 + 1) 162}{(0 + 1) 162 + 120}$$

$$\eta = \underline{57.44\%} \quad \text{efficiency of the butt joint}$$

$$\therefore \underline{\eta = 57.44\%}$$

2) Design a double riveted double strap butt joint for longitudinal steam of boiler of dia 1.3m. with a steam pressure of 2.4 MPa. The working stresses are to be used are 77 MPa in tension, 54 MPa in shear, 120 MPa in crushing, Assume joint efficiency as 81%.

Solⁿ $D = 1.3 \text{ m} = 1300 \text{ mm}$

$P = 2.4 \text{ MPa}$

$\sigma_t = 77$

$\tau = 54$

$\sigma_c = 120$

$\eta = 0.81$

$$t = \frac{P \cdot D}{2 \sigma_t \eta} + C$$

$$= \frac{2.4 \times 1300}{2 \times 77 \times 0.81} + 2$$

$$t = 27.012 \text{ mm} \approx \underline{28 \text{ mm}}$$

ii) $d = 6\sqrt{t}$ to $6.32\sqrt{t}$

$= 31.75$ to 33.46

$\underline{d = 36 \text{ mm}}$

$\left| \begin{array}{l} n_1 = 0 \\ n_2 = 9 \end{array} \right.$

iii) a) $P = \frac{(n_1 + 1.875 n_2) \pi d^2 \tau}{4t \sigma_t} + d$

$P = \underline{131.6 \text{ mm}}$

b) $P = K_1 t + K_2$

$P = 3.5(28) + 41$

$P = \underline{135.5 \text{ mm}}$

iv) $m = 1.5d = \underline{54 \text{ mm}}$

v) $\eta = \frac{P - d}{P} = 72.72\%$

vi) $\eta = \frac{1/4 d^2 (n_1 + 1.875 n_2) \tau}{P + \sigma_t} = 72.42\%$

vii) $\eta = \frac{(n_1 t_1 + n_2) \sigma_c}{(n_1 (t_1/2) + n_2) \sigma_c + \sigma_t} = 75.7\%$

$\left| \begin{array}{l} t_1 = 0.625t \\ t_2 = 1.5t \end{array} \right.$

$\therefore \eta = 72.42\%$

Design procedure for circumferential joints

one plates to be riveted being same in both longitudinal & circumferential joints (t being same)

The diameter of rivets, Transverse pitch & margin are same.

Step 1:- Total steam load $\rightarrow F = \text{Internal dia. Area of pressure vessel} \times \text{Steam pressure}$

$$\therefore F = \left(\frac{\pi}{4} D_i^2 \right) \times P_f$$

Step 2:- strength of each rivet

a) In shear

$$F_s = \frac{\pi}{4} d^2 \tau$$

b) In crushing

$$F_c = d t \sigma_c$$

Step 3:- min strength of rivet $\Rightarrow F_1 = \text{least of above 2 values.}$

Step 3:- no of rivets required = $\frac{\text{Total steam load}}{\text{min. strength of rivet}}$

$$\therefore i = \frac{F}{F_1}$$

Step 4:-

$$\text{Rivets/row} = \frac{\text{Total no of rivets}}{\text{no of rows of rivets}} = \frac{i}{\text{no of rows of rivets}}$$

no of rivets :- 1) For single riveted joint = 1

2) For double riveted joint = 2

Step 5:- pitch of circumferential joint

$$P_c = \frac{\text{Circumference}}{\text{Rivets/rows}} = \frac{\pi D_i}{(\text{rivets/rows})}$$

Step 6 :- efficiencies :-

$$1) \eta_r = \frac{P_c - d}{P_c} \rightarrow \text{plate}$$

$$2) \eta_s = \frac{\eta_1 d^2 (n_1 + 1.875 n_2)}{P_c t \sigma_c}$$

$$3) \eta = \frac{(n_1 \frac{t}{4} + n_2) \sigma_c}{(n_1 \frac{t}{4} + n_2) \sigma_c + \sigma_c}$$

\therefore efficiency (cor) boiler joints is least (or) above 3 values (3 from longitudinal joint & 3 for circumferential joint).

i) Design the main dimension for longitudinal & circumferential joints for boiler whose inner dia is 1.7 m & steam pressure of 2.05 MPa. The rivet in double shear will have an effective resistance not greater than 87.5% over that in single shear. Assume $\sigma_c = 90 \text{ MPa}$, $\sigma_t = 60 \text{ MPa}$

Solⁿ $d = 1.7 \text{ m} = 1700 \text{ mm}$ $\sigma_c = 90 \text{ MPa}$, $\sigma_t = 60 \text{ MPa}$
 η (cor) joint 75%
 $C = 2 \text{ mm}$

$$P = 2.05 \text{ MPa}$$

$$\eta = 0.75$$

$$n = 1 \quad \left\{ \begin{array}{l} \text{for longitudinal joint} \\ n = 2 \end{array} \right.$$

$$i) t = \frac{P \cdot D}{2 \sigma_c \eta} + C$$

$$t = 27.8 \approx 28 \text{ mm}$$

$$ii) d = 6\sqrt{t} \text{ to } 6.325\sqrt{t}$$

$$d = 31.74 \text{ to } 33.46$$

$$d = 33 \text{ mm}$$

$$\text{iii) } P = \frac{(n_1 \pm 1.875 n_2) \pi d^2 z}{h + \sigma_6}$$

$$P = \underline{129.7 \text{ mm}}$$

$$P = R + C$$

2) Design the longitudinal & circumferential joint for a boiler of 2m diameter subjected to a pressure of 1MPa. The longitudinal joint is a triple rivetted butt joint with equal covers & efficiency 85%. The circumferential joint is of double rivetted lap joint. The pitch of the outer row is twice of the pitch of inner row. The yield stress for plate & rivet material is 353MPa. Take FOS = $n = 3$ for tension, FOS = 5 for shear & FOS = 2 for crushing.

Soln: -

✓ For tension

$$D_i = 2\text{m} = 2 \times 10^3\text{mm}$$

$$\sigma_{allt} = \frac{\sigma_y}{n}$$

$$P_f = 1\text{MPa}$$

$$\therefore \sigma_{allt} = \frac{353}{3} = \underline{\underline{117.667\text{MPa}}}$$

$$\eta = 0.85$$

$$\sigma_y = 353\text{MPa}$$

✓ For Shear

~~$$\tau_{all} = \frac{\sigma_y}{2} = \frac{353}{2} = 176.5$$~~

$$\tau_{all} = \frac{\sigma_y}{n} = \underline{\underline{176.5}}$$

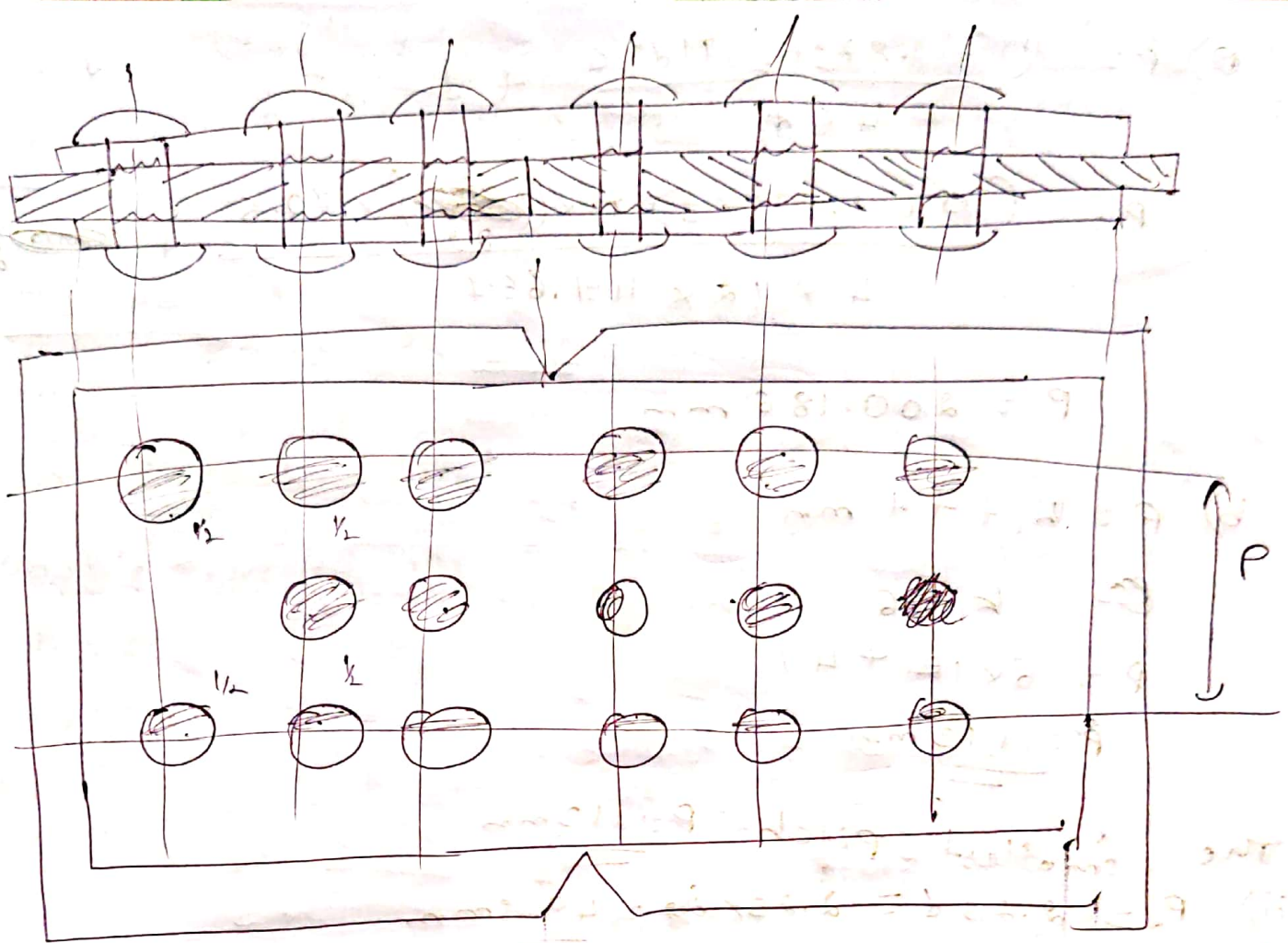
$$\tau_{all} = \frac{353}{5}$$

$$\therefore \tau_{all} = \underline{\underline{70.6\text{MPa}}}$$

✓ For crushing

$$\sigma_c = \frac{\sigma_y}{n} = \frac{\sigma_y}{2} = \frac{353}{2}$$

$$\therefore \sigma_c = \underline{\underline{176.5\text{MPa}}}$$



$$n_1 = 0$$

$$n_2 = 3 + 2$$

$$\therefore n_2 = 5$$

longitudinal

① Thickness of plate (t)

$$t = \frac{P \cdot D_i}{2 \sigma_c \eta} + C$$

$$t = \frac{1 \times 2 \times 10^3}{2 \times 117.667 \times 0.85} + 2$$

Assumed $C = 2$

$$t = 11.998 \text{ mm} = \underline{\underline{12 \text{ mm}}}$$

ii)

$$d = 6 \sqrt{12} \text{ to } 6.325 \sqrt{12}$$

$$d = 20.78 \text{ to } 21.91 \text{ mm}$$

Standard diameter $d = 22$ (table 5.3 (b) Pg 84)

$$i) \quad P = \frac{(n_1 + 1.875n_2) \pi d^3 \tau}{4 \tau \sigma_c} + d$$

$$P = \frac{(0 + 1.875 \times 5) \pi \times \left(\frac{22}{2}\right)^2 \times 70.6}{4 \times 12 \times 117.667} + \frac{22}{2}$$

$$P = 200.186 \text{ mm}$$

$$b) \quad P = k_1 t + 41 \text{ mm}$$

$$k_1 = 6$$

$$P = 6 \times 12 + 41$$

$$P = \underline{113 \text{ mm}}$$

The smallest pitch $P = \underline{113 \text{ mm}}$

$$iii) \quad P_c = 2.25d = 2.25 \times 22 = \underline{49.5 \text{ mm}}$$

$$iv) \quad m = 1.5d = 1.5 \times 22 = \underline{33 \text{ mm}}$$

$$v) \quad t_i = 0.625t = 0.625 \times 12$$

$$t_i = 7.5 \text{ mm} \approx \underline{8 \text{ mm}}$$

$$vi) \quad \eta_p = \frac{P-d}{P} = \frac{113-22}{113}$$

$$\eta_p = 80.53\%$$

$$\eta_s = \frac{\pi d^2/4 (n_1 + 1.875n_2) \tau}{P \tau \sigma_c} = \frac{n(22^2)/4 (0 + 1.875 \times 5) \times 70.6}{113 \times 12 \times 117.667}$$

$$\eta_s = 1.5768 = \underline{157.68\%}$$

$$\eta = \frac{(n_1(t_1/k) + n_2)\sigma_c}{(n_1(t_1/k) + n_2)\sigma_c + \sigma_c} = \frac{(0 + 5)176.5}{(0 + 5)176.5 + 1173.667}$$

$$\eta = 88.23\%$$

$$\eta = 80.53$$

For Circumferential joint

Double rivetted lap joint

$$n_1 = 2$$

$$n_2 = 0$$

$$d = 22\text{mm}$$

i) Total steam $F = \frac{\pi}{4} \times D_i^2 \times P_f$

$$F = \frac{\pi}{4} \times (2 \times 10^3)^2 \times 1$$

$$F = 3.1415 \times 10^6 \text{ N}$$

ii) shear strength of rivet

$$F_s = \frac{\pi}{4} d^2 \tau = \frac{\pi}{4} (22)^2 \times 70.6$$

$$F_s = 26.8373 \times 10^3 \text{ N}$$

Crushing strength of rivet

$$F_c = d t \sigma_c = 22 \times 12 \times 176.5$$

$$F_c = 46.596 \times 10^3 \text{ N}$$

min. strength of rivet $\Rightarrow F_1 = 26.8373 \times 10^3 \text{ N}$

iii) no of required

$$i = \frac{F_c}{F_1} = \frac{3.1415 \times 10^6}{26.8373 \times 10^3}$$

$$i = 114.05703 \approx \underline{\underline{118}}$$

iv) Rivets required per row

$$\text{Rivets/row} = \frac{i}{\text{no of rivets row}} = \frac{118}{2}$$

$$\rightarrow \underline{\underline{59/\text{row}}}$$

v) Circumferential pitch, $P_c = \frac{\pi \times D}{\text{Rivets/row}}$

$$= \frac{\pi \times 2000}{59}$$

$$= \underline{\underline{106.49 \text{ mm}}}$$

$$vi) \eta_p = \frac{P_c - d}{P_c} = \frac{106.49 - 22}{106.49}$$

$$\eta_p = \underline{\underline{79.34\%}}$$

$$\eta_s = \frac{\pi d^2 / 4 (n_1 + 1.875 n_2) \tau}{P_c \times \sigma_c}$$

$$= \frac{\pi (22^2) / 4 (2 + 1.875 \times 1) \times 70.6}{106.49 \times 12 \times 117.667}$$

$$\eta_s = \underline{\underline{35.69\%}}$$

$$\checkmark \eta = \frac{(n_1(t_i/\epsilon) + n_2) \sigma_c}{(n_1 t_i/\epsilon + n_2) \sigma_c + \sigma_f}$$

$$t_i/\epsilon = 1$$

$$\eta = \frac{(2 + 0) \times 176.5}{(2 + 0) 176.5 + 117.667}$$

$$(2 + 0) 176.5 + 117.667$$

~~$$\eta = 524.99\%$$~~

$$\eta = \underline{45.010\%}$$